Notations: Let \mathbb{N} be the set of natural numbers, \mathbb{Z} be the set of integers, \mathbb{R} be the set of real numbers, and let \mathbb{Q} be the set of rational numbers.

1. The number of one-one functions $f: \{1, 2, 3, 4, 5\} \to \{0, 1, 2, 3, 4, 5\}$ such that $f(1) \neq 0$, 1; is

(A) 120

(B) 240

(C) 480

(D) 600

2. Let $f: \mathbb{R} \to \mathbb{R}$ be a continuous function which assumes only rational values, and let $f(\frac{1}{2}) = \frac{1}{2}$. Then

(B) $f(x) = x, x \in \mathbb{R}$.

 $\begin{array}{ll} \text{(A)} & f(x) = \frac{1}{2}, \, x \in \mathbb{R}. \\ \text{(C)} & \text{range of } f \text{ is uncountable} \end{array}$

(D) none of the above

3. The probability that at least one of the two sets A and B occur is 0.6, and that both A and B occur is 0.4. Then the probability that

(A) none of the two sets occur is 0.6

(B) A occurs is 1

(C) B occurs is 0.2

(D) only one of the sets A and B occurs is 0.2

4. The values of the constants A and B so that the function

$$f(x) = \begin{cases} Ax - B, & \text{if } x \le -1\\ 2x^2 + 3Ax + B, & \text{if } -1 < x \le 1\\ 4, & \text{if } x > 1 \end{cases}$$

is continuous for all values of x

(A) $A = \frac{3}{4}, B = -\frac{1}{4}.$ (B) $A = \frac{3}{4}, B = \frac{1}{4}.$ (C) $A = \frac{1}{4}, B = -\frac{3}{4}$ (D) $A = -\frac{1}{4}, B = \frac{3}{4}.$

5. Suppose we have a variable X with mean=10, and variance=9. Consider a linear transformation Y = 2X + 3. Which of the following is true?

(A) mean of Y is 20, variance of Y is 21

(B) mean of Y is 20, variance of Y is 18

(C) mean of Y is 23, variance of Y is 36

(D) mean of Y is 23, variance of Y is 39



7.	Let f be a real-valued function such that $f(0) = -3$ and $f'(x) \le 5$ for all values of x . The largest possible value for $f(2)$ is				
	(A) 7	(B) 8	(C)	, ,	(D) 13
8.	The co-ordinates	of the vertex	of the parabola	$x^2 + 4x + 2y -$	+8 = 0
	(A) (-2,1)	(B) $(-2,2)$	(C) (-2)	,-2) (I	0) (-2,-1)
9.	Consider the fund not correct?	ction $f(x) =$	$ x $ on \mathbb{R} . Which	n one of the fol	lowing is
	(A) f is continuous on \mathbb{R} . (B) f is differentiable on \mathbb{R} . (C) for any real sequence $\{x_n\}$, $\{f(x_n)\} \to 0 \Rightarrow \{x_n\} \to 0$ (D) f is not one-one				
10.	Let f be a function from $\mathbb R$ to $\mathbb R$ such that $f(x)=5x$, if x is rational, and $f(x)=x^2+6$, if x is irrational. Then f is continuous at				;
	(A) 2 only (B)	3 only (C) 2	and 3 (D) all x	in \mathbb{R} such that	$x \neq 2, 3$
11.	Suppose that 5% of men and 0.25% of women are colour-blind. A person is chosen at random and that person happens to be a colour-blind. What is the probability that the person is male? (Assume males and females to be in equal numbers).				
	(A) 0.75	B) 0.90	(C) 0.95	(D) none of t	he above
12.	The three straight lines $2x - 5y + 1 = 0$, $5x + 2y = 0$, and $x - y + 2 = 0$ form			y + 2 = 0	
	(A) a right-an (C) no triangle		` /	n equilateral tr n acute-angle t	_
13.	Let P and Q be constants such that the function $f(x) = x^2 + Px + Q$ has a maximum or minimum at $x = 1$, and $f(1) = 3$. Then the value of Q is				
	(A) -2	(B) 0	(C)) 4	(D) 5

(B) exactly two solutions

(D) no solution

6. The equation $xe^x - 1 = 0$, for $x \in (0, 1)$, has

(A) infinitely many solutions

(C) exactly one solution



14.	If $A = \begin{bmatrix} 2 & 3 \\ 0 & 1 \end{bmatrix}$,	then A^4 is equal	to	
	$(A) \left[\begin{array}{cc} 16 & 9 \\ 0 & 1 \end{array} \right]$	$(B) \left[\begin{array}{cc} 16 & 45 \\ 0 & 1 \end{array} \right]$	$(C) \left[\begin{array}{cc} 16 & 21 \\ 0 & 1 \end{array} \right]$	$(D) \left[\begin{array}{cc} 16 & 81 \\ 0 & 1 \end{array} \right]$
15.	The radius of the	e circle $x^2 + y^2 -$	8x + 6y = 0 is	
	(A) $\sqrt{5}$	(B) $\sqrt{10}$	(C) 5	(D) 10

16. Let A be a $m \times n$ matrix of rank r, where $r < \min\{m,n\}$. Let B be the matrix obtained from A by changing exactly one element. Then the rank of B is

(A)	either r or $r-1$	(B) either r or $r+1$
(C)	either $r-1$ or $r+1$	(D) either $r, r-1$ or $r+1$

17. The number of integers in $\{1,2,3,\ldots,250\}$ that are divisible by at least one of the integers 2, 3 and 5, is

remaining one is
(A) 28 (B) 36 (C) 45 (D) 136

19. The values of λ and μ for which the system of equations x+y+z=6; $x+2y+3z=10; \ x+2y+\lambda z=\mu$ has no solution, are

(A)
$$\lambda = 3, \ \mu = 10$$
 (B) $\lambda \neq 3, \ \mu = 10$ (C) $\lambda = 3, \ \mu \neq 10$ (D) $\lambda \neq 3 \text{ and } \mu \text{ is arbitrary}$

20. Let x,y,z be positive integers such that xyz=8, then the maximum value of $\frac{5xyz}{x+2y+4z}$ is

(A)
$$\frac{40}{35}$$
 (B) $\frac{40}{21}$ (C) $\frac{40}{16}$ (D) $\frac{40}{14}$

21. If $f(x) = \frac{x^2 + (1-x)^2}{\max\{x, 1-x\}}$, then the value of $\int_0^1 f(x) dx$ is (A) $2 \log 2 + \frac{7}{8}$ (B) $2 \log 2 - \frac{1}{2}$ (C) $2 \log 2 - \frac{3}{8}$ (D) $2 \log 2 + \frac{3}{8}$

22.	If n distinct balls, numbered as $1, 2, 3, \ldots, n$, are placed into n cells at random, what is the probability that exactly one cell remains empty?				
	(A) $\frac{n(n-1)}{2n^n}$	_			
23.	Let $f'(x) = g(x)$, function $f^2(x) + g^2$		f(0) = 0,	g(0) = 1, then the	
	(A) constant and (C) strictly increase	•	\ /	stant and equal to 2 ctly decreasing	
24.	The set of all x that	t satisfy $x^5 - x^4$	$-2x^3 \ge 0$ is		

(A) (-1,0] (B) $(2,\infty)$ (C) $[-1,0] \cup [2,\infty)$ (D) $[-1,-\frac{1}{2}] \cup [2,3)$

25. Let
$$f_1(x) = \begin{cases} 8x - 1, & 0 \le x \le 1 \\ 4 + 3x, & 1 \le x \le 2 \end{cases}$$

$$f_2(x) = \begin{cases} 1 + 4x, & 0 \le x \le 1 \\ 3x + 2, & 1 \le x \le 2 \end{cases}$$

(A) n^2

The minimum value of $f(x) = f_1(x)f_2(x)$

(A)
$$-\frac{8}{9}$$
 (B) -1 (C) $-\frac{9}{8}$ (D) none of the above

- 26. In a game of dominoes, each piece is marked with two numbers. The pieces are symmetrical so that the number pair is not ordered, (for example, (2,6)=(6,2)). How many different pieces can be formed using the numbers $1, 2, 3, \ldots, n$? (B) $\frac{n(n-1)}{2}$ (C) $\frac{n(n+1)}{2}$ (D) $\frac{(n+1)(n+2)}{2}$
- 27. If α and β are the roots of the equation $ax^2 + bx + c = 0$, then the roots of the equation $ax^2 + 2bx + 4c = 0$ will be
 - (C) $2\alpha, 2\beta$ (A) α , 4β (B) $4\alpha, \beta$ (D) -2α , -2β
- 28. For qualifying a test, a student has to get a minimum (prefixed) score in each of the 6 subjects. In how many different ways a student can disqualify the test?
 - (C) 2^6 (D) $2^6 - 1$ (A)6!(B) 5!



- 29. Consider the sets A and B, and 0 < P(A), P(B) < 1. If $P(A|B) = P(A|B^c)$, then
 - (A) $P(B|A) = P(B|A^c)$.
- (B) $P(B|A) = P(B^c|A)$
- (C) $P(A \cap B) = P(A)P(B)$.
- (D) $P(B) = P(B^c)$
- 30. If the points (x_1, y_1) , (x_2, y_2) , (x_3, y_3) are collinear, then which of the following is true?
 - (A) $(y_3 y_1)(y_2 y_1) = (x_3 x_1)(x_2 x_1)$
 - (B) $(y_3 y_1)(x_2 x_1) + (x_3 x_1)(y_2 y_1) = 0$
 - (C) $x_1(y_2 y_3) + x_2(y_3 y_1) + x_3(y_1 y_2) = 0$
 - (D) $(x_3 x_1)(y_3 y_1) = (x_2 x_3)(y_2 y_3)$